

PRESENTED AT THE ISCISC'2025 IN TEHRAN, IRAN.

## Evaluating CNF/SMT Encodings for SAT-Based Differential Cryptanalysis of Lightweight Block Ciphers \*\*

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### ARTICLE INFO.

#### Keywords:

Automated Cryptanalysis, CNF, SMT, CVC, Differential Cryptanalysis, Lightweight Block Cipher

#### Type:

#### doi:

### Abstract

This study evaluates three encoding methods for automated differential cryptanalysis: (1) SMT formulations (using CVC), (2) standard CNF, and (3) size-optimised CNF (via Logic Friday). We assess these using four SAT/SMT solver types: single-core (CryptoMiniSat-v5, CaDiCaL), multicore (Treengeling), and massively parallel Mallob—novel to cryptanalysis. Encoding-solver combinations are tested on seven lightweight block ciphers representing distinct design philosophies: SPECK-32 and CHAM-64 (ARX structure), SIMON-32 (AND-RX structure), PRESENT, GIFT-128, and MIDORI-64 (4-bit S-box in SPN structure), and LBLOCK (Feistel structure). For each cipher, SAT/SMT instances targeting specific rounds and differential weights were generated, with wall-clock solving time, parallel efficiency, and modelling effort recorded. Our results establish criteria for optimal encoding-solver pairings that strike a balance between modelling simplicity and computational performance. Crucially, Mallob emerges as the state-of-the-art framework for large-scale automated differential cryptanalysis.

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## 1 Introduction

Differential cryptanalysis [1] remains one of the most fundamental techniques for evaluating the security of symmetric block ciphers. This analysis ex-

amines how input differences propagate through a cipher to produce output differences, with the goal of identifying high-probability differential trails that can be exploited in practical attacks. Over the past two decades, the cryptographic community has invested significant effort in automating the search for such differential characteristics. Declarative frameworks such as Mixed-Integer Linear Programming (MILP) [2, 3], Boolean Satisfiability (SAT), Satisfiability Modulo Theories (SMT) [4–6]. More recently, Constraint Programming (CP) [7–9] has emerged as a powerful tool for automatic trail discovery. These techniques

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\*\*The ISCISC'2025 program committee effort is highly acknowledged for reviewing this paper.

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provide a generic modelling approach, eliminating the need for handcrafted search algorithms. However, each comes with unique trade-offs in terms of modelling complexity, runtime, and scalability.

While MILP-based tools remain widely used for small and mid-sized primitives due to their straightforward support for weight optimisation, SAT and SMT-based approaches have demonstrated superior performance in bit-oriented designs such as SPECK, particularly when solving differential characteristics with tight probabilistic constraints [5]. The work of Bellini *et al.* [10] presents the most comprehensive cross-formalism comparison to date, covering SAT, SMT, MILP, and CP models across more than 20 cryptographic primitives. Their study provides valuable breadth, but it does not deeply investigate the implementation-level aspects of SAT/SMT approaches—such as encoding strategies, modelling compactness, or parallel scalability—which are critical for practical large-scale cryptanalysis.

## Contributions

As SAT/SMT has emerged as the most effective available formalism for automated bit-oriented cryptanalysis, it becomes essential to dissect this approach in detail and analyse its various dimensions, including encoding strategies, solver backends, and scalability aspects. This paper complements and extends prior work by narrowing the focus to SAT/SMT-based differential cryptanalysis and providing a detailed, experimental study at the encoding and solver level. Our contributions are threefold:

- **Encoding-level evaluation.** Unlike [10], which primarily compared different formalisms, we systematically evaluate three concrete encoding strategies—Satisfiability Modulo Theories (SMT-LIB) in the CVC (Cooperating Validity Checker) dialect using bit-vector theories, standard Conjunctive Normal Form (CNF) in DIMACS format, and size-minimised CNF generated by Logic Friday (CNF<sub>LF</sub>, derived from SMT-level encoding)—under identical high-level models. This reveals how modelling choices translate into structural differences in the resulting CNFs and directly affect solver runtime.
- **Solver-level evaluation with parallel scalability.** We assess the performance of these encodings across a diverse solver suite that includes single-core solvers (CryptoMiniSat-v5 [11], CaDiCaL [12]), a multicore portfolio solver (Treengeling [13]), and the massively parallel Mallob platform [14]. Our experiments quantify the impact of solver design (portfolio vs.

decomposition vs. single-core) and demonstrate significant scalability gains, with Mallob achieving an average  $\approx 2.9\times$  speedup over the best single-core baselines.

- **Practical guidelines.** By mapping cipher structures (ARX, SPN, SIMON-like, Feistel) to the most efficient encoding–solver combinations, we extract concrete lessons that serve as a practical guide for future SAT/SMT-based cryptanalysis. This implementation-level perspective provides actionable insights for researchers and designers.

Figure 1 illustrates the overall pipeline, including modelling, encoding evaluation, solver assessment, and results. All modelling scripts, encoding generators, and benchmark configurations are publicly available at: <https://github.com/sat-diff-analysis/differential-sat-encoding.git>

## Outline

The remainder of this paper is organised as follows. Section 2 reviews prior work in automatic differential cryptanalysis, focusing in particular on comparative evaluations of SAT- and SMT-based approaches. In Section 3, we detail the high-level modelling strategy and describe three families of propositional encodings: SMT-LIB (CVC dialect), conventional CNF, and size-minimised CNF produced by Logic Friday (CNF<sub>LF</sub>). Section 4 presents comprehensive experimental results across four solver platforms and seven lightweight block ciphers, comparing performance, parallel scalability, and modelling effort. Finally, Section 5 summarises our key findings and outlines directions for future research.

## 2 Related Work

Sahu *et al.* [6] develop an SMT-based cryptanalysis framework demonstrated on the IDEA cipher. By encoding Boolean representations of the cipher into SMT-LIB, they enable key recovery from a few plaintext-ciphertext pairs. Among several evaluated solvers, Boolector performs best, especially after custom optimisation for modular multiplication.

Delaune *et al.* [15] compare MILP, SAT, CP, and ad-hoc tools for finding differential characteristics in SKINNY. While ad-hoc methods are most effective for truncated trails, CP models outperform others in probability maximisation due to their efficient handling of constraints. Their results improve known bounds for up to 14 rounds.

Sun *et al.* [5] enhance SAT-based differential and linear trail search by encoding Matsui’s bounding conditions directly into SAT without dummy variables.

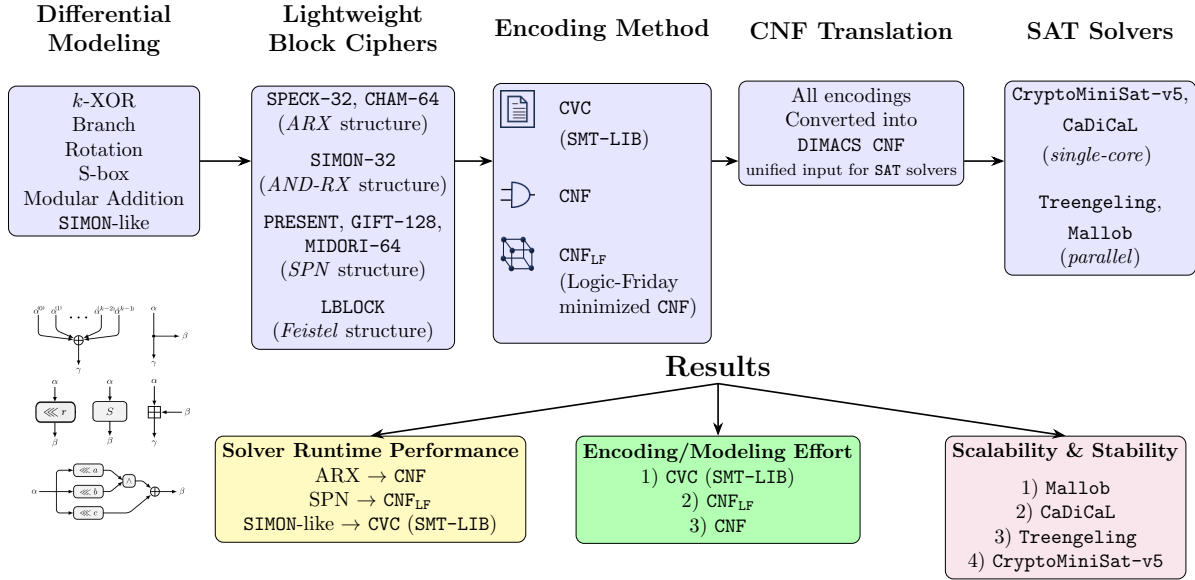


Figure 1. Experimental pipeline for encoding and solver evaluation.

This significantly reduces problem size and improves efficiency, yielding optimal trails for multiple ciphers.

Gundaram *et al.* [16] assess SMT solver performance in key-recovery attacks on SIMON. Although SAT solvers are better for Boolean logic, SMT solvers, particularly Boolector, handle ARX-style constructions more effectively due to their support for word-level operations.

Sun and Wang [17] study modelling strategies for large S-boxes in SAT-based differential cryptanalysis. They introduce logic minimisation techniques that simplify 8-bit S-box encodings, yielding tighter bounds and improved efficiency in the analysis of SKINNY-128 and AES.

Bellini *et al.* [10] provide the most comprehensive comparison to date of four declarative frameworks—SAT, SMT, MILP, and CP—for automatic differential characteristic search in over 20 cryptographic primitives. Their study encompasses three primary tasks: identifying the optimal differential trail, enumerating all optimal trails, and estimating differential probabilities. Employing a diverse suite of 16 solvers across these frameworks, they analyse performance on both easy and challenging instances. Results demonstrate that SAT solvers generally outperform others for ARX and SPN ciphers, with Kissat leading in SAT, Yices2 in SMT, Gurobi in MILP, and Chuffed in CP.

### 3 modelling Primitives

Traditional cryptanalysis has relied on expert intuition and manual inspection, often resulting in limited scalability and inconsistent reproducibility, particu-

larly when analysing ciphers with many rounds. In contrast, automated approaches based on logical reasoning and constraint solving have emerged as powerful alternatives, offering a principled and systematic framework for cryptographic evaluation.

These methods encode cipher components and difference propagation rules into logical formulas that can be processed by SAT and SMT solvers. In SAT-based models, constraints are typically transformed into propositional logic expressed in Conjunctive Normal Form (CNF). SMT-based approaches support richer representations using theories such as bit-vectors, modular arithmetic, and uninterpreted functions. Encodings in SMT-LIB or CVC formats are commonly used by SMT solvers to express operations such as XOR, modular addition, rotations, and S-box transformations more compactly.

Tools like STP act as a bridge between high-level SMT encodings and SAT solvers by translating bit-vector constraints into CNF. This facilitates the use of optimised SAT engines in analysing algebraic structures of block ciphers. SAT solvers such as CryptoMiniSAT v5 and CaDiCaL are widely adopted for their high single-core efficiency and built-in support for features like native XOR clauses and incremental solving. SMT solvers such as Z3 and CVC5 [18] offer enhanced expressiveness at the expense of performance, making them suitable for modelling complex cipher components, like modular addition, in ARX designs.

In multicore settings, parallel solvers like Treengeling, which employ portfolio-based strategies, and distributed systems such as Mallob, which can scale

across thousands of workers using message-passing architectures, facilitate the scalable exploration of large search spaces. These solver backends, combined with expressive encoding strategies, form the computational backbone of modern automated differential and linear cryptanalysis.

In this section, the exclusive OR (XOR) is denoted by  $\oplus$ . Logical OR and AND are represented by  $\vee$  and  $\wedge$ , respectively. Moreover,  $\bar{x}$  denotes the negation of the Boolean variable  $x$ . For rotation amount  $r > 0$ , left and right bitwise rotations are expressed as  $\lll r$  and  $\ggg r$ , respectively.

### 3.1 Logical Encodings of Cryptographic Operations

In this paper, we apply three different logical encodings of CNF expressions to model cryptographic primitives under differential propagation. Each encoding has distinct characteristics and is suited to specific use cases.

#### 1. CVC (High-Level SMT Approach)

The CVC format is widely used in SMT solvers such as CVC5 and Boolector. It supports rich data types, including bit-vectors, arrays, and integer arithmetic, making it suitable for expressing cryptographic operations directly in a high-level, human-readable form. For instance, an  $n$ -bit XOR operation ( $\gamma = \alpha \oplus \beta$ ) can be encoded as follows:

```
"ASSERT (gamma=BVXOR(alpha,beta));"
```

This encoding abstracts away the underlying CNF representation, allowing for rapid prototyping. Integrating with tools like CryptoSMT is beneficial for automating differential and linear cryptanalysis.

#### 2. DIMACS CNF (Low-Level SAT Format)

DIMACS CNF is the standard format used by SAT solvers, where variables are represented by positive integers (e.g., 1, 2, 3,...), and negation is denoted by a minus sign (e.g., -1). A DIMACS file starts with a header line of the form:

```
p cnf <num_vars> <num_clauses>
```

This specifies the number of variables and clauses. Each subsequent line represents a clause consisting of space-separated literals, ending with a zero to indicate termination. For example, the XOR operation can be modelled using four clauses per bit position:

```
p cnf 3 4
1 2 -3 0
1 -2 3 0
```

```
-1 2 3 0
-1 -2 -3 0
```

### 3. CNF<sub>LF</sub> (Hybrid Logic Friday-Inspired Encoding)

The CNF<sub>LF</sub> method is inspired by the output of the logic minimisation tool Logic Friday. This approach translates each clause extracted from Logic Friday into individual ASSERT statements in SMT-LIB format, making it compatible with solvers such as Z3 or Boolector.

This method enables seamless integration of CNF-based logical constraints into automated reasoning frameworks, facilitating tasks such as differential cryptanalysis. An example of generating bitwise XOR constraints ( $\gamma = \alpha \oplus \beta$ ) programmatically is shown below:

```
for i in range(n):
"ASSERT
  ((({0}[{3}:{3}])
 |({1}[{3}:{3}])
 |(~{2}[{3}:{3}])
 )=0bin1);".
  format(alpha,
    beta, gamma, i)
"ASSERT
  ((({0}[{3}:{3}])
 |(~{1}[{3}:{3}])
 |({2}[{3}:{3}])
 )=0bin1);".format
  (alpha, beta,
    gamma, i)
"ASSERT
  (((~{0}[{3}:{3}])
 |({1}[{3}:{3}])
 |({2}[{3}:{3}])
 )=0bin1);".format
  (alpha, beta,
    gamma, i)
"ASSERT
  (((~{0}[{3}:{3}])
 |(~{1}[{3}:{3}])
 |(~{2}[{3}:{3}])
 )=0bin1);".
  format(alpha,
    beta, gamma, i)
```

Each line corresponds to one clause from the CNF representation of XOR. These clauses enforce the deterministic behaviour of XOR under differential propagation:  $\gamma_i = \alpha_i \oplus \beta_i$ .

### 3.2 modelling Differential Propagation of Operations

This section presents the logical models for linear and nonlinear cryptographic operations under differential propagation. We use  $x_i$  to denote the  $i$ -th bit of an  $n$ -bit vector  $x$ , indexed from 0 (MSB).



### $k$ -XOR Operation

The XOR of  $k+1$  binary variables refers to an  $k$ -XOR operation. Our approach to modelling  $k$ -XOR avoids the use of dummy variables. This modelling employs integer programming constraints derived from the convex hull of XOR outcomes, as applied in [19].

For a  $k$ -XOR operation applied bitwise to  $n$ -bit words, let  $\alpha^{(0)}, \dots, \alpha^{(k)}$  be input differences  $\gamma$  be the output difference. A differential  $(\alpha^{(0)}, \dots, \alpha^{(k)}, \gamma)$  is valid if and only if the following CNF formula is satisfied for all bit positions  $0 \leq i < n$ :

$$\bigwedge_{S \subseteq \{0, \dots, k\} : |S| \text{ is odd}} \left( \bigvee_{j \in S} \overline{\alpha_i^{(j)}} \vee \left( \bigvee_{j \notin S} \alpha_i^{(j)} \vee \gamma_i \right) \right) \wedge \bigwedge_{S \subseteq \{0, \dots, k\} : |S| \text{ is even}} \left( \bigvee_{j \in S} \overline{\alpha_i^{(j)}} \vee \left( \bigvee_{j \notin S} \alpha_i^{(j)} \vee \overline{\gamma_i} \right) \right)$$

In particular, the 2-XOR modelling approach is applied to the SIMON algorithm and the matrix multiplication layer of the MIDORI-64 algorithm.

### Branching Operation

For an  $n$ -bit branching operation, let  $\alpha$  denote the input difference and  $\beta, \gamma$  represent the output differences on each branch. A differential  $(\alpha, \beta, \gamma)$  is valid if and only if the following CNF formula is satisfied for all bit positions  $0 \leq i < n$ :

$$(\overline{\alpha_i} \vee \beta_i) \wedge (\alpha_i \vee \overline{\beta_i}) \wedge (\overline{\alpha_i} \vee \gamma_i) \wedge (\alpha_i \vee \overline{\gamma_i}).$$

This enforces the deterministic behaviour of the branching operation:  $\alpha_i = \beta_i = \gamma_i$ .

### Rotation Operation

For an  $n$ -bit rotation operation, let  $\alpha$  denote the input difference and  $\beta$  represent the output difference after rotating by  $r$  bits. A differential  $(\alpha, \beta)$  is valid if and only if the following CNF constraints are satisfied for all bit positions  $0 \leq i < n$ :

- Left rotation by  $r$ :

$$(\overline{\alpha_{(i-r) \bmod n}} \vee \beta_i) \wedge (\alpha_{(i-r) \bmod n} \vee \overline{\beta_i})$$

- Right rotation by  $r$ :

$$(\overline{\alpha_{(i+r) \bmod n}} \vee \beta_i) \wedge (\alpha_{(i+r) \bmod n} \vee \overline{\beta_i})$$

### S-box Layer

We first generate the *Difference Distribution Table* (DDT) of the S-box. The DDT of an S-box  $S : \mathbb{F}_2^n \rightarrow \mathbb{F}_2^n$  is a  $2^n \times 2^n$  matrix where each entry  $\text{DDT}(\alpha, \beta)$  for  $\alpha \in \mathbb{F}_2^n$  (input difference) and  $\beta \in \mathbb{F}_2^n$  (output difference) is defined as:

$$\text{DDT}(\alpha, \beta) = |\{x \in \mathbb{F}_2^n \mid S(x) \oplus S(x \oplus \alpha) = \beta\}|$$

This denotes the number of inputs  $x$  for which an input difference  $\alpha$  results in an output difference  $\beta$  after application of the S-box  $S$ . From the DDT, two main representations are extracted:

-  $\star$ -DDT: A binary representation indicating whether a differential transition  $(\alpha, \beta)$  is possible or impossible [20].

-  $w$ -DDT: A weighted version where each entry represents either the number of occurrences or the probability of a given differential transition [10].

Let  $F$  be a flag indicating whether the transition is valid. For  $\star$ -DDT-based modelling, the format of the truth table is  $(\alpha, \beta, w, F)$ , where  $w = 0$  if and only if it corresponds to impossible or deterministic transitions. For  $w$ -DDT-based modelling, the format extends to  $(\alpha, \beta, p_1, \dots, p_k, F)$ , where  $p_1, \dots, p_k$  are dummy Boolean variables used to encode the differential weight  $w = -\log_2(p)$ , where  $p$  denotes the probability of a given differential  $(\alpha, \beta)$ . Let  $P$  contain all probabilities of valid differentials. The weight  $w$  is decomposed into two components [17]:

- An integer part, encoded using  $\mu$  Boolean variables  $u = (u_0, \dots, u_{\mu-1})$ , where  $\mu = \max_{p \in P} (\lceil -\log_2(p) \rceil)$ ,
- A fractional part, represented by  $k$  Boolean variables  $v = (v_0, \dots, v_{k-1})$ , corresponding to the following set of size  $k$ :

$$D = \{\lceil -\log_2(p) \rceil - (-\log_2(p)) \mid -\log_2(p) \notin \mathbb{Z}, p \in P\}$$

If  $\alpha \rightarrow \beta$  is a possible differential propagation with a probability of  $p$ , then the corresponding assignments to  $\alpha \parallel \beta \parallel u \parallel v$  must satisfy the equation:

$$\sum_{i=0}^{\mu-1} u_i + \sum_{i=0}^{k-1} d_i \cdot v_i = -\log_2(p),$$

where  $d_i$  is the  $i$ -th member of  $D$ . The resulting truth tables are then fed into **LogicFriday**, a logic minimisation tool that automatically translates them into (CNF) expressions.

### Modular Addition

For an  $n$ -bit modular addition operation  $z = x + y \bmod 2^n$ , let  $\alpha$  and  $\beta$  denote the input differences and  $\gamma$  represent the output difference. A differential  $(\alpha, \beta, \gamma)$  is valid if it satisfies the differential constraints for modular addition defined in [21], including:

$$\alpha_{n-1} \oplus \beta_{n-1} = \gamma_{n-1}$$

and for  $0 \leq i < n-1$ ,

$$\begin{aligned}
 & (\alpha_i \vee \beta_i \vee \overline{\gamma_i} \vee \alpha_{i+1} \vee \beta_{i+1} \vee \gamma_{i+1}) \\
 & \wedge (\alpha_i \vee \overline{\beta_i} \vee \gamma_i \vee \alpha_{i+1} \vee \beta_{i+1} \vee \gamma_{i+1}) \\
 & \wedge (\overline{\alpha_i} \vee \beta_i \vee \gamma_i \vee \alpha_{i+1} \vee \beta_{i+1} \vee \gamma_{i+1}) \\
 & \wedge (\overline{\alpha_i} \vee \overline{\beta_i} \vee \overline{\gamma_i} \vee \alpha_{i+1} \vee \beta_{i+1} \vee \gamma_{i+1}) \\
 & \wedge (\alpha_i \vee \beta_i \vee \gamma_i \vee \overline{\alpha_{i+1}} \vee \overline{\beta_{i+1}} \vee \overline{\gamma_{i+1}}) \\
 & \wedge (\alpha_i \vee \overline{\beta_i} \vee \overline{\gamma_i} \vee \overline{\alpha_{i+1}} \vee \overline{\beta_{i+1}} \vee \overline{\gamma_{i+1}}) \\
 & \wedge (\overline{\alpha_i} \vee \beta_i \vee \overline{\gamma_i} \vee \overline{\alpha_{i+1}} \vee \overline{\beta_{i+1}} \vee \overline{\gamma_{i+1}})
 \end{aligned}$$

The logarithmic weight  $w$  of a differential is computed using dummy variables  $w_0, w_1, \dots, w_{n-2}$ , where:

$$w = \sum_{i=0}^{n-2} w_i$$

with  $w_i = 1$  if and only if  $\alpha_i$ ,  $\beta_i$ , and  $\gamma_i$  are not all equal. For  $0 \leq i \leq n-2$ , each  $w_i$  must satisfy:

$$\begin{aligned}
 & (\alpha_{i+1} \vee \gamma_{i+1} \vee w_i) \wedge (\beta_{i+1} \vee \gamma_{i+1} \vee w_i) \\
 & \wedge (\alpha_{i+1} \vee \beta_{i+1} \vee w_i) \wedge (\alpha_{i+1} \vee \beta_{i+1} \vee \gamma_{i+1} \vee w_i) \\
 & \wedge (\alpha_{i+1} \vee \beta_{i+1} \vee \gamma_{i+1} \vee w_i) \wedge (\alpha_{i+1} \vee \beta_{i+1} \vee \gamma_{i+1} \vee w_i)
 \end{aligned}$$

### SIMON-like Round Function

The round function of SIMON is defined over  $n$ -bit words and takes the form

$$f(x) = ((x \lll a) \wedge (x \lll b)) \oplus (x \lll c),$$

where  $a > b$ ,  $n$  is even, and  $\gcd(n, a-b) = 1$ . We apply the differential model from [22], which is adapted for automated analysis using SAT/SMT solvers [5].

Let  $\alpha$  and  $\beta$  denote the input and output differences, respectively. To capture the propagation patterns through the AND operation, three dummy  $n$ -bit variables  $z$ ,  $varibits$ ,  $doublebits$  are used. When  $\alpha$  is not the all-ones vector (a special case requiring separate analysis), the differential transition  $(\alpha, \beta)$  is considered valid if and only if all of the following CNF constraints are satisfied across every bit position  $0 \leq i \leq n-1$  (with all indices computed modulo  $n$ ):

$$\begin{aligned}
 & (\overline{\alpha_{i+a}} \vee varibits_i) \wedge (\overline{\alpha_{i+b}} \vee varibits_i) \\
 & \wedge (\alpha_{i+a} \vee \alpha_{i+b} \vee varibits_i) \wedge (varibits_i \vee \overline{z_i}) \\
 & \wedge (\overline{\alpha_{i+a}} \vee \overline{\alpha_{i+b}} \vee doublebits_i) \\
 & \wedge (\overline{\alpha_{i+b}} \vee \alpha_{i+2a-b} \vee doublebits_i) \\
 & \wedge (\alpha_{i+a} \vee \overline{\alpha_{i+b}} \vee \overline{\alpha_{i+2a-b}} \vee doublebits_i) \\
 & \wedge (\alpha_{i+b} \vee doublebits_i) \wedge (doublebits_i \vee z_i \vee \overline{z_{i+a-b}}) \\
 & \wedge (doublebits_i \vee \overline{z_i} \vee z_{i+a-b}).
 \end{aligned}$$

Furthermore, the necessary 2-XOR differential constraints for  $\alpha_{i+c} \oplus \beta_i \oplus z_i$ .

### 3.3 Objective Function

In automated differential cryptanalysis using SAT or SMT solvers, a crucial step is defining an objective

function that guides the search toward trails with higher probabilities. This is typically achieved by introducing dummy binary variables  $w_i \in \{0, 1\}$ , where each variable encodes the contribution of a specific operation to the overall weight of a differential trail. Let  $u$  be the number of weight variables. The goal is to minimise the total weight  $\sum_{i=0}^{u-1} w_i$ .

Since standard SAT solvers do not directly support optimisation objectives, we instead impose a constraint on the total weight:

$$\sum_{i=0}^{u-1} w_i \leq k,$$

where  $k$  is a user-defined upper bound on the total weight. This constraint can be efficiently encoded into CNF using the *sequential encoding method* [23], which introduces dummy variables  $u_{i,j}$  (with  $0 \leq i \leq u-2$ ,  $0 \leq j \leq k-1$ ) to enforce the cardinality limit. The following clauses ensure that any assignment violating the weight limit results in an unsatisfiable formula:

$$\begin{aligned}
 & (w_0 \vee u_{0,0}) \wedge (u_{0,j}) \wedge (w_i \vee u_{i,0}) \wedge (u_{i-1,0} \vee u_{i,0}) \\
 & \wedge (w_i \vee u_{i-1,j-1} \vee u_{i,j}) \wedge (u_{i-1,j} \vee u_{i,j}) \\
 & \wedge (w_i \vee u_{i-1,w-1}) \wedge (w_{u-1} \vee u_{u-2,w-1})
 \end{aligned}$$

for  $1 \leq i \leq u-2$ ,  $1 \leq j \leq k-1$ . These clauses effectively restrict the number of active weight variables to at most  $k$ , ensuring that the solver explores only promising trails.

Unlike SAT solvers, modern SMT solvers, such as CVC5 and Z3, support native optimisation objectives. This allows us to minimise the total weight directly without manually imposing bounds via cardinality constraints. For example, in the CVC and CNF<sub>LF</sub> format, we can define bit-vector variables representing the weight contributions and then minimise their sum:

```

VAR
k : BITVECTOR(u);
w_0, w_1, ..., w_(u-1) : BITVECTOR(1)
"ASSERT(k=BVPLUS(u, w_0, w_1, ..., w_(u-1)))";
MINIMISE k
    
```

## 4 Experimental Results

In this section, we present and compare experimental results for seven lightweight block ciphers. Each cipher is analysed separately over selected round ranges and differential weight bounds using a unified modelling and solving framework. The full results are summarised in Table 1, where each row corresponds to a specific cipher, round range, weight range, and encoding. For each such configuration, the table reports the average runtime of four different solvers as separate columns.

Three encoding strategies are considered: SMT-LIB-style CVC, standard conjunctive normal form (CNF), and size-optimised CNF<sub>LF</sub> generated by Logic Friday, all of which are ultimately converted to CNF before being passed to the SAT solver. These encodings are evaluated using four solver backends: `CryptoMiniSat v5`, `CaDiCaL`, `Treengeling`, and the massively parallel `Mallob` system. For each encoding-solver combination, we report the average wall-clock runtime over five independent executions to reduce stochastic variance. In the case of `CryptoMiniSat-v5` and `Treengeling`, only one run is reported for some ciphers due to excessive runtime. For others, even a single execution did not complete within a reasonable time limit, as indicated by the “-” symbol in [Table 1](#). To ensure the correctness of our differential models, output probabilities and weight computations have been cross-validated against trusted reference works [5, 24].

The round and weight bounds for each cipher were selected based on two practical considerations: (1) computational feasibility, as full exploration across all round counts and weight combinations would be prohibitively time-consuming, and (2) runtime visibility, since later-round instances typically incur higher solving times, making performance differences between solvers more observable and the comparisons more informative.

All experiments were conducted on a desktop machine running Ubuntu 22.04.5 LTS with the Linux kernel 6.8.0. The system is equipped with a 13th Gen Intel<sup>®</sup> Core<sup>™</sup> i7-13700K processor (24 threads, up to 5.4 GHz turbo boost) and 64 GiB of RAM. Benchmarks were performed in a single-user environment to ensure resource consistency.

#### 4.1 Results on SPECK-32

SPECK-32 is a lightweight ARX-based block cipher introduced by the NSA in 2013 [25]. It operates on 32-bit blocks using modular addition, XOR, and rotations, and consists of 22 rounds with a 64-bit key.

For SPECK-32, the differential analysis was performed over the range 15–17 rounds, with weight bounds selected from 50 to 63. Within this range, rounds 15, 16, and 17 were found to be SAT for weights 54, 58, and 63, respectively, while all lower weights in each round resulted in UNSAT outcomes. As a representative example, the SMT-LIB CVC model for round 17 at weight 63 resulted in 16,590 variables and 47,174 clauses; the standard CNF encoding yielded 16,833 variables and 36,412 clauses; and the Logic Friday-optimised CNF<sub>LF</sub> version contained 26,535 variables and 77,009 clauses. Among all tested configurations, the combination of CNF encoding with the

parallel `Mallob` solver yielded the best performance in terms of runtime efficiency.

#### 4.2 Results on CHAM-64

CHAM-64 is a lightweight ARX-based block cipher [26, 27], designed for resource-constrained devices. It employs a 4-branch generalised Feistel structure with 88 rounds.

For this cipher, the differential weight range of 39 to 46 was selected. Within this range, rounds 29 to 31 correspond to satisfiable weights 41, 43, and 46, respectively. As a representative case, for the final satisfiable instance at weight 46 and round 31, the CVC encoding leads to 37,332 variables and 102,824 clauses; the CNF encoding results in 22,369 variables and 48,811 clauses; and the CNF<sub>LF</sub> encoding yields 52,987 variables and 149,789 clauses. The best-performing encoding-solver pair in terms of solving time for this cipher is CNF combined with `Mallob`.

As illustrated in [Figure 2](#), the solving time per differential weight is shown for each encoding-solver pair. It can be observed that CNF combined with `Mallob` achieves the lowest solving time across almost all weights. Additionally, SAT solvers tend to perform significantly faster when the problem instance is satisfiable, highlighting the importance of satisfiability in runtime behaviour.

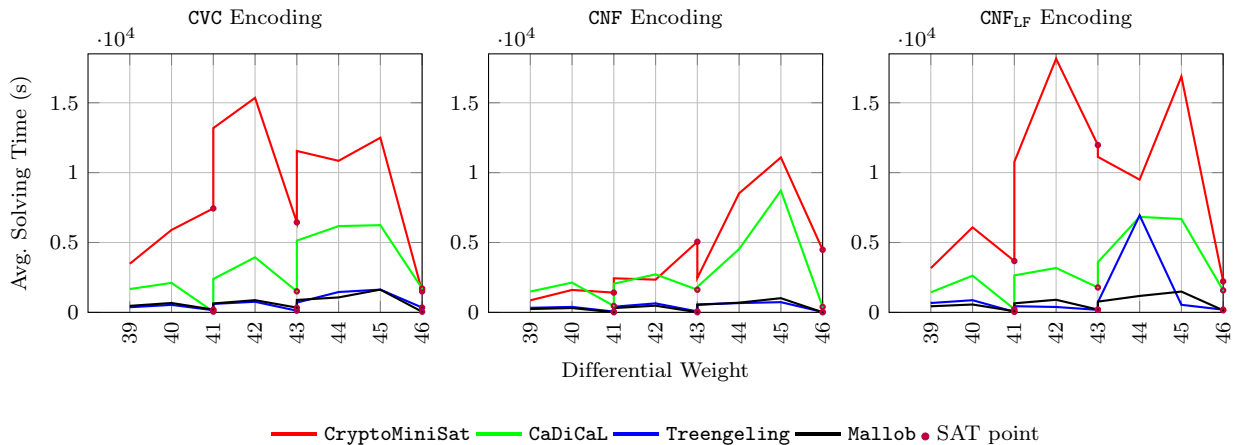
#### 4.3 Results on SIMON-32

SIMON-32 is a lightweight block cipher proposed by the NSA [25]. It uses a Feistel structure over 32 rounds, operating on 32-bit blocks with a 64-bit key. The design employs only simple bitwise operations—AND, XOR, and left circular shifts—optimised for hardware efficiency.

For this cipher, the differential weight range of 80 to 90 was selected. Within this range, rounds 30 to 32 correspond to satisfiable weights 84, 86, and 90, respectively. As a representative case, for the final satisfiable instance at weight 90 and round 32, the CVC encoding results in 60,873 variables and 176,327 clauses; the CNF encoding produces 49,094 variables and 104,690 clauses; and the CNF<sub>LF</sub> encoding yields 55,465 variables and 157,031 clauses. The best-performing encoding-solver pair in terms of runtime for this cipher is CVC combined with `Mallob`. [Figure 3](#) clearly illustrates this observation, demonstrating that CVC consistently results in lower solving times across different differential weights.

**Table 1.** Unified comparison of encoding strategies and solver run-times for seven lightweight block ciphers across selected rounds and differential weight bounds.

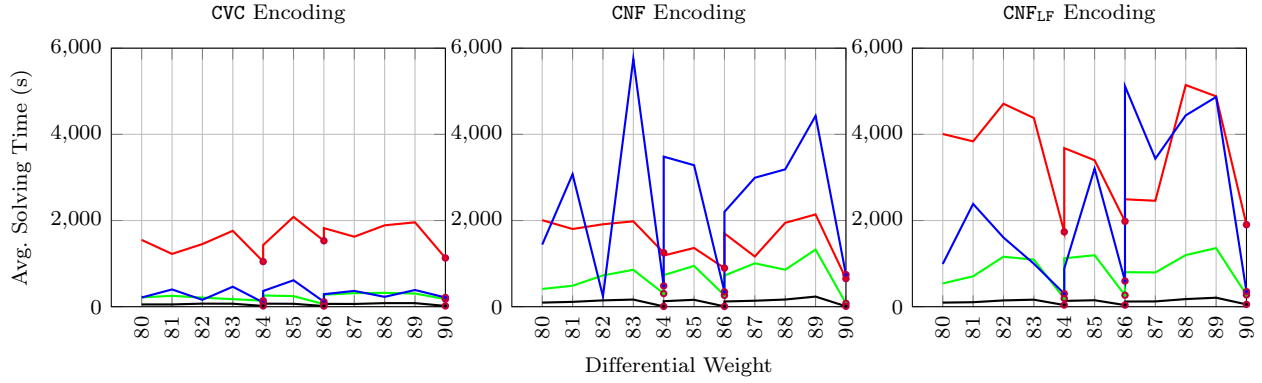
| Cipher    | Rounds | $w$     | Encoding          | $T_{\text{CryptoMiniSat}}$ (s) | $T_{\text{CaDiCaL}}$ (s) | $T_{\text{Treengeling}}$ (s) | $T_{\text{Mallob}}$ (s) |
|-----------|--------|---------|-------------------|--------------------------------|--------------------------|------------------------------|-------------------------|
| SPECK-32  | 15–17  | 50–63   | CVC               | –                              | 72688.92                 | 450815.29                    | 28961.95                |
|           |        |         | CNF               | –                              | 26510.69                 | 27827.62                     | <b>16773.82</b>         |
|           |        |         | CNF <sub>LF</sub> | –                              | 61419.44                 | 132351.23                    | 28002.53                |
| CHAM-64   | 29–31  | 39–46   | CVC               | 88191.15                       | 30920.49                 | 6670.23                      | 6813.53                 |
|           |        |         | CNF               | 40265.00                       | 25930.79                 | 3882.11                      | <b>3604.28</b>          |
|           |        |         | CNF <sub>LF</sub> | 93539.85                       | 30584.30                 | 10981.80                     | 6408.91                 |
| SIMON-32  | 30–32  | 80–90   | CVC               | 20505.68                       | 2956.85                  | 3914.43                      | <b>727.70</b>           |
|           |        |         | CNF               | 20008.64                       | 8722.44                  | 31350.13                     | 1490.26                 |
|           |        |         | CNF <sub>LF</sub> | 44615.49                       | 10704.35                 | 30731.87                     | 1547.23                 |
| PRESENT   | 29–31  | 124–136 | CVC               | 27466.68                       | 10155.67                 | 34933.00                     | 3532.13                 |
|           |        |         | CNF               | 40042.46                       | 9110.09                  | 92383.47                     | 2448.33                 |
|           |        |         | CNF <sub>LF</sub> | 24674.96                       | 6916.66                  | 17925.05                     | <b>2383.09</b>          |
| GIFT-128  | 10–13  | 45–67   | CVC               | 502515.59                      | 50215.32                 | –                            | 21549.09                |
|           |        |         | CNF               | 209664.23                      | 54195.14                 | –                            | 14587.91                |
|           |        |         | CNF <sub>LF</sub> | 435965.99                      | 40737.46                 | –                            | <b>14312.07</b>         |
| MIDORI-64 | 14–16  | 135–168 | CVC               | –                              | 17664.82                 | 140832.67                    | 10160.83                |
|           |        |         | CNF               | –                              | 16565.82                 | 201050.68                    | 5278.16                 |
|           |        |         | CNF <sub>LF</sub> | –                              | 13686.85                 | 107484.33                    | <b>4684.26</b>          |
| LBLOCK    | 27–29  | 121–135 | CVC               | 28784.45                       | 2960.65                  | 9718.11                      | 2427.87                 |
|           |        |         | CNF               | 21165.68                       | 4684.28                  | 23929.41                     | 1589.65                 |
|           |        |         | CNF <sub>LF</sub> | 48227.89                       | 2059.20                  | 7461.84                      | <b>1271.40</b>          |


**Figure 2.** Comparison of average solving time per differential weight for CHAM-64 using different encoding strategies and SAT solvers. Filled circles highlight SAT results. Each subplot shows one encoding with solvers.

#### 4.4 Results on PRESENT

PRESENT is a well-known 64-bit lightweight block cipher designed for hardware efficiency, proposed by Bogdanov *et al.* [28]. It follows an SPN structure with 4-bit S-boxes and a bitwise permutation, supporting 80- and 128-bit keys over 31 rounds.

For PRESENT, the differential search was carried out over rounds 29–31 with weight bounds ranging from 124 to 136. Within this range, rounds 29, 30, and 31 were found to be SAT at weights 128, 132, and 136, respectively, while all lower weights for each round were UNSAT. As a representative case, the



**Figure 3.** Comparison of average solving time per differential weight for SIMON-32 using different encoding strategies and SAT solvers. Filled circles highlight SAT results. Each subplot shows one encoding with solvers.

CVC SMT representation for round 31 at weight 136 contains 1,552,022 variables and 4,773,255 clauses; the standard CNF encoding consists of 205,768 variables and 433,096 clauses; and the CNF<sub>LF</sub> encoding yields 75,577 variables and 303,103 clauses. Among all tested solver–encoding combinations, the fastest execution was achieved using the CNF<sub>LF</sub> encoding paired with the Mallob parallel solver.

#### 4.5 Results on GIFT-128

GIFT-128 is a 40-round lightweight block cipher based on an SPN structure [29]. It operates on 128-bit blocks using 4-bit S-boxes, a fixed bit permutation, and round-dependent key and constant injection.

For GIFT-128, the differential characteristic search was conducted over rounds 10–13 within the weight interval of 45 to 67. In this setting, the SAT results were observed for weights 49, 54, 60, and 67 corresponding to rounds 10, 11, 12, and 13, respectively, while lower weights yielded UNSAT outcomes. As an illustrative example, the CVC SMT-based formulation for round 13 at weight 67 comprises 656,793 variables and 2,067,862 clauses; the standard CNF encoding includes 86,589 variables and 190,743 clauses; and the CNF<sub>LF</sub> representation yields 60,533 variables and 236,943 clauses. The best overall performance in terms of solver runtime was achieved using the CNF<sub>LF</sub> encoding in conjunction with the parallel Mallob backend.

#### 4.6 Results on MIDORI-64

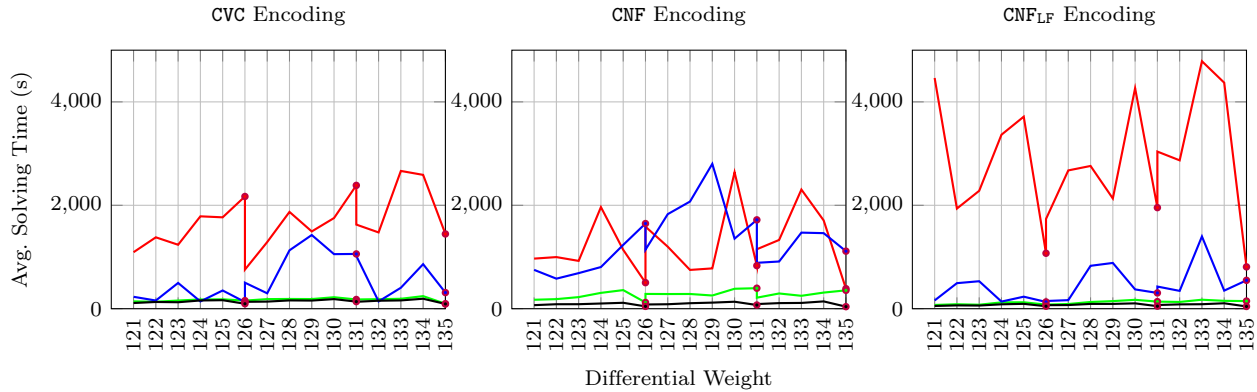
MIDORI-64 is a lightweight 64-bit block cipher [30], targeting resource-constrained environments. It follows an SPN structure and supports two key sizes: 128 and 64 bits. MIDORI-64 uses a single 4-bit involutive S-box and a lightweight almost-MDS matrix for diffusion, designed to minimise energy consumption while offering competitive security margins.

For MIDORI-64, differential SAT-based exploration was performed over rounds 14–16 within the weight interval of 135 to 168. SAT results were obtained for weights 144, 150, and 168, corresponding to rounds 14, 15, and 16, respectively, while all lower weights yielded UNSAT verdicts. For the final weight tested—168 at round 16—the CVC representation comprises 3,145,065 variables and 9,422,663 clauses; the standard CNF encoding contains 131,736 variables and 280,584 clauses; and the optimised CNF<sub>LF</sub> form yields 121,945 variables and 354,071 clauses. The fastest runtime across all solver–encoding combinations was achieved using CNF<sub>LF</sub> paired with the Mallob solver.

#### 4.7 Results on LBLOCK

LBLOCK is a lightweight 64-bit block cipher proposed in 2011 [31]. It follows a 32-round Feistel structure, using a 4-bit S-box and a simple bit permutation for diffusion. Its low area footprint makes it suitable for constrained devices such as RFID and sensor networks.

For LBLOCK, differential search experiments were conducted across rounds 27–29 over the weight interval 121 to 135. SAT results were obtained for weights 126, 131, and 135 corresponding to rounds 27, 28, and 29, respectively, while other weight–round pairs in this range were UNSAT. For the final weight tested—135 at round 29—the CVC format includes 2,853,345 variables and 8,545,871 clauses; the standard CNF encoding comprises 97,369 variables and 202,624 clauses; and the optimised CNF<sub>LF</sub> encoding yields 83,178 variables and 236,066 clauses. The best-performing encoding–solver combination in terms of runtime was CNF<sub>LF</sub> with the Mallob solver. Figure 4 reflects this trend, showing the solving time per differential weight for each encoding–solver pair.



**Figure 4.** Comparison of average solving time per differential weight for LBLOCK using different encoding strategies and SAT solvers. Filled circles highlight SAT results. Each subplot shows one encoding with solvers.

### 5 Discussion and Conclusion

This study has presented a comprehensive empirical evaluation of encoding methodologies and solver frameworks for automated differential cryptanalysis. Three distinct encodings - Satisfiability Modulo Theories (SMT) in the CVC dialect, standard Conjunctive Normal Form (CNF), and size-optimised CNF<sub>LF</sub> generated via Logic Friday - have been rigorously benchmarked against seven diverse lightweight block ciphers (SPECK-32, CHAM-64, SIMON-32, PRESENT, GIFT-128, MIDORI-64, LBLOCK) using four classes of SAT/SMT solvers (CryptoMiniSat-v5, CaDiCaL, Treengeling, and Mallob).

Although every model is ultimately solved in CNF, the resulting formula depends strongly on the encoding path. Across our benchmarks, we observed clear shifts in variable and clause counts, preservation of XOR/parity relations, gate decomposition and auxiliary signals, and the way the minimum-weight objective is encoded.

These structural differences steer CDCL dynamics (unit propagation per decision, conflict frequency, VSIDS/LBD statistics) and thereby runtime. For example, in PRESENT and GIFT-128, CNF<sub>LF</sub> reduced the number of variables but produced more, shorter clauses, which improved propagation and led to faster solves; in contrast, for ARX ciphers such as SPECK-32 and CHAM-64, the raw CNF often performed better. Detailed counts and timings supporting these observations appear in Section 4.

Our results have established concrete criteria for selecting optimal encoding-solver pairings, balancing modelling simplicity with computational performance. Crucially, the massively parallel framework Mallob has emerged as the state-of-the-art solution for large-scale differential cryptanalysis tasks, delivering an average speedup of  $\approx 2.9$  over the best single-core baseline across our benchmarks.

Furthermore, our solver-specific analysis reveals that multicore parallelisation does not inherently guarantee superior performance over single-threaded approaches. While one might expect multi-threaded solvers to outperform their single-core counterparts consistently, our results in Table 1 contradict this intuition.

Notably, CaDiCaL—a single-threaded, general-purpose SAT solver—outperforms the cryptography-focused CryptoMiniSat-v5 and even surpasses the multi-threaded Treengeling in several configurations, underscoring the significance of efficient pre-processing and clause learning techniques over mere parallelism. That said, Treengeling’s performance tends to improve when solving structurally larger problems or ciphers with more expansive search spaces, where its decomposition strategy can better exploit available cores.

In the multicore category, Treengeling employs a decomposition-based strategy, partitioning the input formula into multiple subproblems that are solved concurrently using shared-memory threads. However, this approach often fails to scale effectively in our cryptanalytic benchmarks. In contrast, Mallob adopts a portfolio-style parallelism model: it launches multiple instances of single-threaded solvers (e.g., Kissat, CaDiCaL, Lingeling), each seeded differently but solving the same problem instance. Clause learning is coordinated via a centralised communication backend, enabling efficient knowledge sharing across workers. Although Mallob does not decompose the input structurally, it consistently outperforms both single-threaded and decomposition-based frameworks, making it the most robust solution for differential cryptanalysis workloads in our evaluation.

For all Mallob-based experiments, we utilised the `kc1` portfolio configuration, which cyclically assigns each thread to a different backend solver (Kissat,

CaDiCaL, Lingeling), further enhancing solver diversity and reducing search space overlap across threads.

Furthermore, the investigation has revealed a significant structural dependency in encoding efficiency: For S-box-based ciphers (e.g., PRESENT, GIFT-128, MIDORI-64, LBLOCK), the CNF<sub>LF</sub> encoding consistently yields the fastest solving times, with the objective modelled as a direct sum of weight contributions. Conversely, for ARX-based constructions (SPECK-32 and CHAM-64), standard CNF modelling proves empirically superior, with the weight-minimisation objective enforced via cardinality constraints encoded using the sequential counter encoding method.

Notably, based on the results presented in Section 4.3, for SIMON-like ciphers, the CVC encoding consistently demonstrates superior performance in terms of solving time. This is primarily due to the nature of the SIMON-like round function, which includes an AND operation with dependent inputs. In the CVC encoding, such functions can be efficiently modelled using conditional constructs (e.g., IF statements) without introducing dummy variables. In contrast, both CNF and CNF<sub>LF</sub> encodings require additional dummy variables to represent the same logic, leading to larger and more complex formulas that degrade solver performance.

As an empirically grounded guideline, use CNF for ARX, CNF<sub>LF</sub> for SPN, and CVC for SIMON-like block ciphers; pair the model with Mallob by default for time-to-solution and robustness, and fall back to CaDiCaL when constrained to a single core.

In terms of modelling effort, the CVC encoding is the most convenient due to its higher-level abstraction, followed by CNF<sub>LF</sub> and then standard CNF, which requires more manual formulation.

These findings guide researchers in making more efficient implementation choices for analyzing and designing cipher structures vulnerable to differential attacks. Classifying encodings by cipher structure can significantly reduce cryptanalysis time. Further improvements may come from refining the CNF encoding of the weight-minimisation objective, which strongly affects solver performance.

Promising avenues for future work include extending this methodology to other cryptanalytic attacks (e.g., linear, integral) and systematically identifying efficient solver-encoding combinations for each specific attack type on broader classes of cryptographic primitives. Moreover, while SAT-based approaches are highly effective for bit-oriented lightweight ciphers, they are less suitable for more complex designs such as AES. In particular, bit-level SAT modelling of 8-bit S-boxes leads to an explosion in variables and clauses,

making direct analysis inefficient; in such cases, MILP or CP formulations are generally more practical. Extending our systematic evaluation to word-oriented industrial standards such as AES and ChaCha remains an important direction for future work.

## Acknowledgment

This work is based upon research funded by Iran National Science Foundation (INSF) under project No.4026442.

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